

George Washington Carver High School of Engineering and Science 2021 Summer Enrichment

Due date: 8/31/21

DIRECTIONS/INFORMATION:

- The Summer Enrichment must be completed in its entirety over the summer.
- This assignment will count as a test grade for the first marking period. Late submissions will reduce the grade earned.
- This packet contains math skills required for Pre-Algebra.
- The packet is divided into eight, one-week sections that will allow you to develop a schedule for completing the packet. Follow the directions given in each section of the packet carefully.

Thank you in advance for completing this packet by 8/31/21.

Supplies for this course:

- -1" binder (3-ring)
- -Loose-leaf Paper
- -Pencils

-Calculator: TI-84 Plus (expensive but highly recommended) or TI-30XIIS





Week 1: Decimal and Fraction Operations

| Adding & Subtracting Decimals | | |
|--|-----|--------------|
| 1. Write the problem vertically, lining up the decimal points. | | |
| 2. Add additional zeroes at the end, if necessary, to make the numbers have the same number of decimal places. | ex: | 14.2 - 7.934 |
| 3. Add/subtract as if the numbers are whole numbers | | - 7.934 |
| 4. Bring the decimal point straight down | | 6:266 |



- 1. Write the dividend under the long division symbol and the divisor to the left of it.
- 2. Move the decimal point in the divisor after the number to turn it into a whole number and then move the decimal in the dividend the same number of places. Then bring it up.
- 3. Divide as if the numbers are both whole numbers.
- 4. Annex zeros in the dividend as needed until there is no remainder. If your answer is a repeating decimal, write the answer using bar notation.



0.3

Evaluate each expression.

| 1. 5.983 + 2.99 | 2. 224 - 56.73 | 3. 6.12 - 4.923 |
|------------------------|----------------------------|--------------------------|
| 4. 24 . 5 · 3.2 | 5. 0.23 · 7 | 6. 3.86 · 9.15 |
| 7. 4.8 ÷ 5 | 8. 46.3 ÷ 1.5 | 9. 147 ÷ 2.25 |
| 10. 24.33 - 2.5 · 7 | 11. 3.9 + 4.5 ² | 12. 9.25(18.4 - 2 · 1.2) |

Solve each word problem, showing all work.

| 13. Jeff had \$46.18 in his wallet Monday morning. He gave half of his money to his brother. He then bought two donuts for \$0.75 each and a cup of coffee for \$2.99. How much money did Jeff have left? 14. Five friends split a \$65.20 bill at a restaurant. They also each left \$2.75 for the tip. How much money did each person pay in all? | | | - | The second | |
|--|-----|---|-----|---|--|
| | 13. | Jeff had \$46.18 in his wallet Monday morning. He gave half of his money to his brother. He then bought two donuts for \$0.75 each and a cup of coffee for \$2.99. How much money did Jeff have left? | 14. | Five friends split a \$65.20 bill at a restaurant. They also each left \$2.75 for the tip. How much money did each person pay in all? | |

Adding Fractions & Mixed Numbers

ex: $3\frac{3}{4} + 2\frac{1}{2}$

ex: $5\frac{1}{4} - 1\frac{2}{3}$

 $3\frac{3}{4} = 3\frac{3}{4}$

 $5\frac{5}{11} = 6\frac{1}{4}$

 $5\frac{1}{4} = 5\frac{3}{12} = 4\frac{15}{12}$

 $1\frac{2}{3} = 1\frac{8}{12} = 1\frac{8}{12}$

3 12

- 1. Find a common denominator for the two fractions.
- 2. Add the two numerators and keep the denominator the same.
- 3. Add the whole numbers.
- 4. Simplify the answer and/or change improper fraction answers to mixed numbers.

Subtracting Fractions & Mixed Numbers

- 1. Find a common denominator for the two fractions.
- 2. Subtract the two numerators and keep the denominators the same. If the top numerator is smaller than the bottom numerator, borrow from the whole number and rename the top fraction.
- 3. Subtract the whole numbers.
- 4. Simplify the answer.



Dividing Fractions & Mixed Numbers 1. Turn any mixed numbers and whole numbers into improper fractions. 2. Keep the first fraction the same, change the division to multiplication, and flip the second fraction to its reciprocal. 3. Multiply the fractions. 4. Simplify the answer and/or change improper fraction answers to mixed numbers. $\frac{7}{1} \div \frac{7}{4} = \frac{4}{1} = 4$

Evaluate each expression.

| 15. 4/5 + 3/4 | 16. 4 2 + 2 4 14 | 17.8 11 + 9 <u>5</u> 18 |
|--|---|---------------------------------------|
| 18. 6 - 3 | $19.8\frac{3}{5} - 2\frac{1}{3}$ | 20. $4\frac{1}{6} - \frac{8}{9}$ |
| 21. $\frac{4}{25} \cdot \frac{15}{16}$ | 22. 2 ³ / ₄ · 8 | 23. $6\frac{5}{8} \cdot 3\frac{1}{2}$ |
| 24. $\frac{7}{9} \div \frac{2}{3}$ | 25. 4 ÷ 10 | $26.5\frac{2}{3} \div 2\frac{5}{6}$ |

Solve each word problem, showing all work.

| 27. | Jaimie ran $3\frac{1}{2}$ miles on Monday. She ran half as far on Tuesday as she did on Monday. How far did Jaimie run in all on Monday and Tuesday? | 28. | A $5\frac{1}{2}$ quart pot is filled $\frac{2}{3}$ of the way with water. How many more quarts of water can the pot hold? |
|-----|---|-----|--|
| | | | |

Week 2: Ratios and Proportions

| Ratio | 08 |
|--|--|
| Ratios are comparisons of two quantities. | ex: write the ratio of triangles to circles |
| Fraction (A) | in 3 ways: 🔺 🛦 🛦 🔿 🔿 |
| | |
| - Colon (A:B) - Word Form (A to B) | $\frac{4}{2} = \frac{2}{2} + \frac{2}$ |
| | 2 7 2 10 1 |
| Ratios can be simplified just like fractions. | |
| Rates & (| Unit Rates |
| Rates are ratios that compare quantities measured in A unit rate is a rate with a denominator of 1. | different units. ex: express as a unit rate: 125 miles in 4 hours |
| To convert a rate to a unit rate: | 125 mi |
| 1. Divide the numerator by the denominator | $\frac{125 \div 4}{125 \div 4} = 31.25$ |
| 2. Either write your answer as a fraction with a labe numerator and denominator OR as one number la unit "per" the second unit | I for the both the beled with the first $\frac{31.25 \text{ mi}}{1 \text{ hr}}$ or 31.25 miles per hr |
| To convert a: Fractions, De | cimals, & Percent |
| - Decimal to Percent: move the decimal point 2 pla | ces to the right ex: $0.345 = 34.5\%$ |
| - Percent to Decimal: move the decimal point 2 pla | ces to the left $ex: \sqrt{7\%} = 0.07$ |
| - <u>Decimal to Fraction</u> : write the decimal over the plu digit and then simplify | ace value of the last ex: $0.008 = \frac{8}{1000} = \frac{1}{125}$ |
| - Fraction to Decimal: divide the numerator by the | denominator $ex: \frac{1}{5} = 5$ 1.0 |
| - <u>Percent to Fraction</u> : write the percent over 100 a | nd then simplify ex: $45\% = \frac{45}{100} = \frac{9}{20}$ |
| - <u>Fraction to Percent</u> : convert the fraction to a dec convert the decimal to a perc | ent ex: $\frac{3}{10} = 0.3 = 30\%$ |
| Percent of | a Number |

Turn the percent to a fraction or decimal.
 Multiply the fraction/decimal by the number.

ex: Find 18% of 40 $0.18 \cdot 40 = 7.2$

| 29. A bank contains 15 pennies and 12 nickels. Write the ratio of nickels to pennies. | 30. A bowl contains 6 apples and some bananas. If there are a total of 10 pieces of fruit, find the ratio of apples to bananas. |
|--|---|
|--|---|

Convert each rate to a unit rate.

| 31. \$4.25 for 64 fluid ounces | 32. 297 miles on 11 gallons of gas | 33. 124 feet in 10 seconds |
|--------------------------------|------------------------------------|----------------------------|
| | | |
| | | |
| | | |

Complete the chart by converting each number to a percent, fraction, and/or decimal.

| | Fraction | Decimal | Percent |
|-----|----------|---------|---------|
| 34. | 3 8 | | |
| 35. | | 0.45 | |
| 36. | | | 72% |
| 37. | | 0.1 | |
| 38. | 3 200 | | |

Find each percent of a number.

| 39. 30% (| of 90 | 40. 15% of 38 | 41. 50% of 86 |
|-----------|--------|---------------|---------------|
| 42. 75% (| of 160 | 43. 24% of 35 | 44. 2% of 74 |

| Unit: NUMBER RELATIONSHIPS and COMPUTATION | | |
|---|--|--|
| Objective: Identify and determine equivalent forms of proper fractions as decimals, percents, and ratios - A. | | |
| Examples: Write $\frac{21}{25}$ as a decimal | ne en energe de la Colle de Blance e Blance e de la Reference de Statistica e de College de la College | |
| Method 1: | Method 2: Divide 21 by 25 | |
| Change $\frac{21}{2}$ to a fraction with a denominator of 10, 100, or 1000 | 0.04 | |
| 25 | $\frac{21}{21} \rightarrow 25\overline{)21.00}$ | |
| EX: $\frac{21}{25} = \frac{1}{100}$ | 25 25)21100 | |
| 25 100 | $\frac{-200}{100}$ | |
| (Use 100, since 25 divides into 100 evenly) | 100 | |
| $\frac{21}{21} = \frac{x4}{x^2} = \frac{84}{x^2} = \frac{84}{x^2} = 0.84$ as a decimal | <u>-100</u> | |
| 25 x4 100 100 | 21 | |
| | Therefore: $\frac{21}{25} = 0.84$ | |
| | 7 | |
| 1.) Write $\frac{1}{20}$ as a decimal. Use method 1 | 2.) Write $\frac{-}{8}$ as a decimal. Use method 2. | |
| | | |
| | | |
| | | |
| | | |
| | | |
| | | |
| 3.) Write $\frac{3}{2}$ as a decimal Use method 2 | 4.) Write $\frac{27}{2}$ as a decimal Use method 2 | |
| 16 | 40 | |
| | | |
| | | |
| | | |
| | | |
| | | |
| | | |
| 5.) Write $-$ as a decimal. Use method 1 4 | 6.) Write $-$ as a decimal. Use method 1 5 | |
| | | |
| | | |
| | V12 = | |
| | | |

| Unit: NUMBER RELATIONSHIPS and COMPUTATION | | |
|--|---|--|
| Objective: Identify and determine equivalent forms of proper fractions as decimals, percents, and ratios - B. | | |
| | | |
| Key Concept: Percent (%) is a ratio that compares a numb | per to 100 | |
| | | |
| Fraction to Percent: | Percent to fraction: | |
| 19 | EX: Change 75% to a fraction in simplest form | |
| EX : Change $\frac{15}{25}$ to a percent | | |
| Since % means out of 100 19 ? | 75% means 75 out of 100 | |
| Since % means out of 100, $\frac{1}{25} = \frac{1}{100}$ | 75 | |
| 19 x4 76 | $75\% = \frac{75}{100}$ Write the percent as a fraction with a denominator of 100 | |
| $\frac{1}{25} = \frac{1}{100}$ | 100 with a denominator of 100 | |
| 76 760 | 75 . 05 . 0 | |
| $\frac{100}{100} = 76\%$ | $\frac{75 \div 25}{100} = \frac{3}{100}$ Simplify | |
| | $100 \div 25 4$ | |
| 1.) Change $\frac{17}{22}$ to a percent | 2.) Change 84% to a fraction in simplest form | |
| 20 | | |
| | | |
| | | |
| | | |
| | | |
| | | |
| | | |
| | | |
| 3.) Change $\frac{3}{1}$ to a percent | 4.) Change 90% to a fraction in simplest form | |
| 4 | | |
| | | |
| | | |
| | | |
| | | |
| | | |
| | | |
| | | |
| 5) luon answered ²⁴ substitute service | 6) 78% of the class completed their homework last | |
| 5.) Juan answered $\frac{1}{25}$ questions correctly on his quiz. | night What fraction of the class completed their | |
| What percent of the guestions did he get correct? | homework? | |
| | | |
| Æ | | |
| A CONTRACTOR OF THE OFFICE OFF | The second se | |
| | Jac N | |
| | | |
| | 2 (B) | |
| | | |

Week 3: Number System and Geometry Part 1

Comparing Integers

Integers are numbers without fractional parts. They can be positive, negative, or zero. The further right a number is on the number line, the greater it is.



The absolute value of a number is the distance the number is from zero.



q

-7

 $-q \leftarrow The absolute value of -q = q$





Compare the integers with <, >, or =.

| 454 🔿 -5 | 46. 2 🔿 -2 | 47. -5 () 5 | 487 🔿 6 | 4913 -9 |
|---------------|------------|----------------|------------|----------------|
| 50. -7 🔿 -6 | 5117 -14 | 52. -3 -2 | 53. 0 🔵 -6 | 54. -4 () 6 |

Graph and label each of the ordered pairs in the coordinate plane. Then state the quadrant or axis in/on which the point is located.

| Lasta and the state of the | | |
|----------------------------|---------------|---|
| 55. A(2, 4) | 56. B(0, -3) | |
| 57. C(1, -1) | 58. D(3, 3) | |
| 59. E(-4, I) | 60. F(2, 0) | |
| 61. G(-3, -2) | 62. H(-2, 3) | |
| 63. I(0, 2) | 64. J(-1, -4) | |
| | | • |

Find the perimeter, area, and/or volume of the given figure.



Week 4: Geometry Part 2



| Unit: KNOWLEDGE of MEASUREMENT Objective: Determine the missing measure of a square or re number dimensions. | ectangle given the area using whole |
|--|---|
| The area (A) of a rectangle or square can be found by mu The missing measure of a square or rectangle can be dete | Itiplying the length (I) by the width (w). A = I x w rmined by using division. |
| Examples: | |
| $ \begin{array}{cccc} A = I \times w \\ \hline & w & \underline{64} = \underline{16} \times w \\ \hline & 16 & 16 \\ \end{array} $ | |
| A = 64 cm ² 4 = w | The width of the rectangle is 4 cm. |
| 1.) Determine the missing side of the square. Please show your work. A = 81 cm² w = 9 cm 3.) Determine the missing side of a rectangle with an area of 144 cm² and a width of 8 cm. Please show your work. | 2.) Determine the missing side of the rectangle. Please show your work. 5 cm A = 65 cm² / = 4.) Determine the missing side of a rectangle with an area of 480 cm² and a length of 32 cm. Please show your work. |
| 5.) Marcus plans to paint a bright green rectangle on the bottom of his pool. He has enough paint to cover an area of 273 square feet. He wants the width of the rectangle to be 13 feet. Determine what the length of the rectangle should be. Please show your work. | 6.) Brianna wants to put stickers, to celebrate her birthday, on top of chocolate bar wrappers. The bar is 48 mm wide and has an area of 4128 mm ² . What must be the length of the sticker to cover the top of the bar? |

Week 5: Expressions and Equations

Evaluating Algebraic Expressions

- 1. Substitute the given numbers for the variables
- ex: evaluate x + 4y for $x = 4 \mathcal{E} y = 6$ 4 + 4(6)

2. Evaluate the expression using the order of operations

4 + 24 = 28



One-Step Multiplication & Division Equations

- <u>Multiplication Equations</u>: Divide both sides of the equation by the number next to the variable



n = 50

- <u>Division Equations</u>: Multiply both sides of the equation by the number under the variable

Problem Solving

- 1. Read the problem. Identify the question that is being asked and the key information in the problem.
- 2. Plan how you are going to solve the problem and estimate the answer.
- 3. Solve the problem using the strategy of your choice.
- 4. Check your answer. Make sure your answer is reasonable and compare it to your estimate. Label your answer with appropriate units.

Evaluate each expression for a = 5, b = 12, c = 10, $\varepsilon d = 2$.

| 71. 2b - a | 72. d(ab – c) | 73. 3 + $\frac{b}{d}$ |
|-----------------|---------------|-----------------------|
| | | |
| | | |
| an table of | | |
| 74. 4a b+ 4d | 75. 2a² – c | 76. b-c+d |
| | | |
| | | |
| | | |

Solve each one-step equation.

| 77. g + 3 = 17 | 78. r - 6 = 7 | 79. 6b = 18 | 80. $\frac{h}{q} = 3$ |
|------------------------|---------------------|-------------------------|-------------------------|
| 81. 5 = f − 8 | 82. 48 = 12b | 83. a + 24 = 83 | 84. 17 + x = 23 |
| $85. 10 = \frac{m}{5}$ | 86. 86.5 = f - 7.63 | 87. <mark>n</mark> = 11 | $88. \frac{3}{4}h = 12$ |



| In a multiplicati equation 2x = Multiplication e | ion equation, the number by wh 8, the coefficient is 2. equations: Divide both sides by t | ich a variable is multiplied is the coefficient so that the two | called the coefficient . In the multiplication o sides remain equal. |
|---|---|--|--|
| In a division eq 4 is the diviso Division equation | uation, the number by which the or. ons: Multiply both sides of the ed | e variable is divided is called quation by the divisor so that | the divisor . In the division equation $\frac{x}{4}$, t the two sides remain equal. |
| Examples: | | | |
| 4b = 16 origina | l equation | $\frac{m}{6} = 11$ | original equation |
| 4 4 divide | both sides by 4 | $6 \times \frac{m}{6} = 11 \times 6$ | multiply each side by 6 |
| 1b = 4 solutio b = 4 simplif | n y | $\frac{1m}{m} = \frac{66}{66}$ | solution simplify |
| 1.) | 7x = 63 | 2.) | $\frac{k}{9} = 8$ |
| 2) | | | |
| 5.) | 5b = 3.55 | 4.) | $\frac{n}{7} = 5.55$ |
| 5.) | | 6.) | |
| | 12m = 84.72 | | $\frac{p}{13}$ = 2.67 |
| 4 | | | |

Week 6: Word Problems

Solve each word problem using the method of your choice.

| 89. A fencing company charges \$22 per foot to install a wood fence. How much will it cost to install a wood fence around a rectangular pool area that is 20 feet wide and 38 feet long? | 90. A 6 inch-tall plant grew 34 of an inch one week and twice as much the following week. How tall is the plant now? |
|---|--|
| 91. Jack can read 45 pages of his book in one and a half hours. At that rate, how long will it take him to read the entire 300-page book? | 92. Brian ordered 3 large cheese pizzas and a salad. The salad cost \$4.95. If he spent a total of \$47.60 including the \$5 tip, how much did each pizza cost? (Assume there is no tax). |
| 93. A cookie recipe calls for 3 ¹ / ₄ cups of flour. The recipe makes 3 dozen cookies. How much four is needed to make 144 cookies? | 94. Ella has a box of chocolate candies. She gives $\frac{1}{3}$ of the candies to her sister, 4 to her brother, and she eats the remaining 12 candies. How many chocolate candies were in the box originally? |

Week 7: Statistics

| Unit: KNOWLEDGE of STATISTICS Objective: Determine the measures of cent | tral tendency (mean, median, and mode) and the range. |
|--|--|
| A number that helps describe all of the da The mean is the sum of the data divided by The median is the middle number of the ord The mode is the number or numbers that of The range is the difference between the gree | ta in a data set is a measure of central tendency . the number of pieces of data. dered data (least to greatest.) ccur most often. eatest and least values of the data set. |
| Examples: F | ind the mean, median, mode, and range of the data. /lean = <u>25 + 34 + 39 + 41 + 45 + 52 + 27 + 22 + 56 + 61 + 15 + 27</u> 12 |
| Jacket Prices (\$) | = <u>444</u> = 37 The mean price of a jacket is \$37. 12 |
| 25 34 39 41 45 52 27 22 | Median = 15 22 25 27 27 34 39 41 45 52 56 61 (data ordered) |
| 30 01 13 27 | $\frac{-34+39}{2} = 36.5$ The median price of a jacket is \$36.50. |
| | Mode = \$27 because it is the only piece of data that occurs more than once. |
| | Range = 61 – 15 = \$46 |
| 1.) Find the mean, median, mode, and rang of data. 6, 9, 2, 4, 3, 6, 5 | 2.) Find the mean, median, mode, and range for each set of data. 13, 7, 17, 19, 7, 15, 11, 7, 21 |
| | |
| 3.) Find the mean, median, mode, and rang of data. 28, 32, 23, 43, 32, 27, 21, | of data. 34 157, 124, 157, 124, 157, 139 |
| | X = 2/1123 |

Exercises: <u>SHOW ALL WORK.</u>

Find the **mean**, **median**, **range**, **and mode** of each of the following data sets. You may use a calculator to identify the mean.

a. 54, 65, 74, 35, 87 b. 54.6, 45.98, 67.4, 55.6, 45.7, 58.9

c. 122, 145, 156, 176, 198, 202 d. 11, 14, 16, 15, 32, 23, 27, 27, 23, 43

e. 6, 7, 8, 4, 6, 5, 8, 3, 6, 8, 5, 4

f. -4, 7, -3, 4, 8, 12, -5, -3, 8, 16, 9

f. 43, 56, 98, 67, 87

h. 12, 15, 14, 18, 33, 32, 24, 26, 27

Week 8: Performance Task #1 Apply skills and Explain your thinking!

Alisa hopes to play beach volleyball in the Olympics someday. She has convinced her parents to allow her to set up a beach volleyball court in their backyard. A standard beach volleyball court is approximately 26 feet by 52 feet. She figures that she will need the sand to be one foot deep. She goes to the hardware store to shop for sand and sees the following signs on pallets containing bags of sand.



a. What is the rate that Brand A is selling for? Give the rate and then specify the unit rate.

b. Which brand is offering better value? Explain your answer.

c. Alisa uses her cell phone to search how many pounds of sand is required to fill 1 cubic foot and finds the answer is 100 pounds. Choose one of the brands and compute how much it will cost Alisa to purchase enough sand to fill the court. Identify which brand was chosen as part of your answer. Use the volume formula, V = I • w • h, to determine your answer.

Week 9: Performance Task #2 Apply skills and Explain your thinking!

Loren and Julie have different part-time jobs after school. They are both paid at a constant rate of dollars per hour. The tables below show Loren and Julie's total income (amount earned) for working a given amount of time.

Loren

| Hours | 2 | 4 | 6 | 8 | 10 | 12 | 14 | 16 | 18 |
|---------|----|----|----|----|----|-----|----|----|-----|
| Dollars | 18 | 36 | 54 | 72 | 90 | 108 | | | 162 |

Julie

| Hours | 3 | 6 | 9 | 12 | 15 | 18 | 21 | 24 | 27 |
|---------|----|---|-----|-----|-----|-----|----|-----|-----|
| Dollars | 36 | | 108 | 144 | 180 | 216 | | 288 | 324 |

- a. Find the missing values in the two tables above.
- b. Who makes more per hour? Justify your answer.

- c. Write how much Julie makes as a rate. What is the unit rate?
- d. How much money would Julie earn for working 16 hours?
- e. What is the ratio between how much Loren makes per hour and how much Julie makes per hour?
- f. Julie works $\frac{1}{12}$ hours/dollar. Write a one or two-sentence explanation of what this rate means. Use this rate to find how long it takes for Julie to earn \$228.

Student Evaluation/Reflection Form

Complete this form after finishing the summer math challenge

1. How would you rate the difficulty of the problems in general throughout the summer math challenge? Please rate on a scale from 1-10, with 1 being the easiest and 10 being the hardest.

| (e | 1 asiest) | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 (hardest) |
|------------|--------------------|-------------------|-------------------------|----------------------|--------------------|---------|---------------------|-------------------|-----------------------|----------------------------------|
| Wha | t types | of prob | lems in [.] | the cho | allenge | were th | ne most | difficult | and w | /hy? |
| Wha | t types | of prob | plems in ⁻ | the cho | allenge | were th | ne easie | st and v | vhy? | |
| Whe | n did yo lenge? | ou com (Did yo | iplete th iu do it e | ie chall every de | enge? ay, onc | How dia | d you po ek, com | ace you pleted | irself w it in a f | hen completing the Tew days?) |
| List a | it least (| 3 goals | you hav | ve for 71 | h-grad | e math | | | | |
| 1 2 |) | | | | | | | | | |
| 3 Explo |) | you pla | an to ac | chieve t | hose go | oals. | | | | |
| | | | | | | | | | | |
| | | | | | | | | | | |

Thank you for taking the time to complete this evaluation/reflection! I really appreciate your input!